



# First principles modeling of oxygen vacancy formation and mobility in (Ba,Sr)(Co,Fe)O<sub>3-δ</sub> perovskites

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State Research  
Stuttgart

## Ba<sub>1-x</sub>Sr<sub>x</sub>Co<sub>y</sub>Fe<sub>1-y</sub>O<sub>3-δ</sub> perovskites: high concentration and mobility of V<sub>O</sub><sup>••</sup>

BSCF permeation membranes

⇒ high *D* (Z.P. Shao (2000))

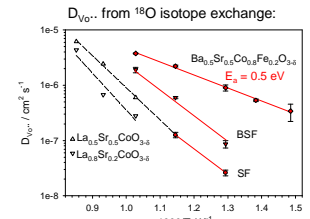
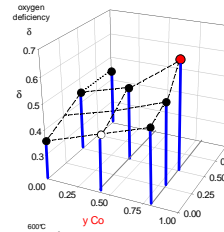
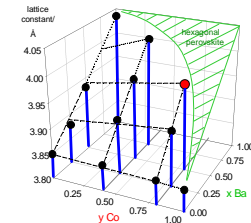
test as SOFC cathode

⇒ high *k* (Z.P. Shao, S.M. Haile (2004))

mechanistic interpretation:

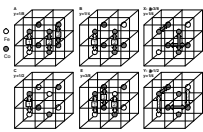
L. Wang, R. Merkle, J. Maier

J. Electrochem. Soc. 157 (2010) B1802



L. Wang et al., *Appl. Phys. Lett.* 94 (2009) 071908  
LSC: R. De Souza et al., *Solid State Ionics* 106 (1998) 175

## Computational details

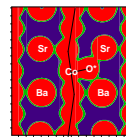


different vacancy configurations in supercell

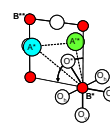
- \* VASP 4.6 + PAW and plane wave basis set
- \* PBE-type exchange-correlation GGA functional
- \* 4x4x4 k-point mesh in the Brillouin zone (Monkhorst-Pack scheme)
- \* ion charges calculated by the Bader method
- \* energy cut-off 520 eV
- \* Ba<sub>2</sub>Sr<sub>4</sub>(Co,Fe)<sub>4</sub>O<sub>12.5</sub> supercells (2x2x2)
- \* Fe: high spin state, Co: intermediate spin

E. A. Kotomin et al., *Solid State Ionics* 188 (2011) 1

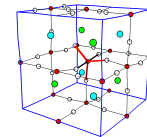
## Oxygen vacancy migration



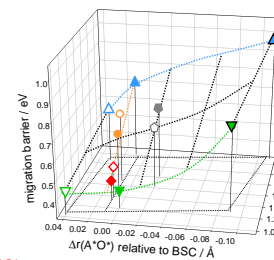
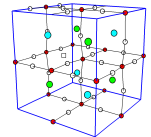
transition state:  
e density map in (110) plane  
for Ba<sub>0.5</sub>Sr<sub>0.5</sub>Co<sub>0.75</sub>Fe<sub>0.25</sub>O<sub>2.875</sub>



transition state:  
O<sup>••</sup> moving through  
"critical triangle"



transition state  
and  
initial state  
for Ba<sub>0.5</sub>Sr<sub>0.5</sub>Co<sub>0.5</sub>O<sub>2.875</sub>



BSF: Sr<sup>••</sup> F<sup>••</sup> V<sup>••</sup> ▲  
BaSr<sup>••</sup> F<sup>••</sup> V<sup>••</sup> ▲  
BaBa<sup>••</sup> F<sup>••</sup> V<sup>••</sup> ▲  
BSCF5528: BaSr<sup>••</sup> F<sup>••</sup> V<sup>••</sup> ●  
BSCF5555: BaSr<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ○  
SCF: Sr<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ○  
BSCF: BaSr<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ◆  
BaSr<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ◆  
BSC: Sr<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ▼  
BaSr<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ▼  
BaBa<sup>••</sup> C<sup>••</sup> V<sup>••</sup> ▼

geometric factors:  
d<sub>A<sup>••</sup>-O<sup>••</sup></sub> compared to BSC<sup>••</sup>  
(cf. SrSr, SrBa and BaBa barriers for BSC)

electronic factors:  
vacancy formation energy  
(cf. SrBa barriers for BSC, SCF, BSF)

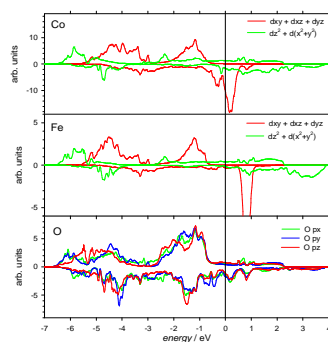
barriers	DFT	expt.	good agreement
BSCF	0.44 eV	0.5 eV*	
BSF	0.72 eV	1.0 eV*	
SCF	0.64 eV	0.65 eV**	

\* L. Wang et al., *JES* 157 (2010) B1802

\*\* Y. Teraoka et al., *Mat. Res. Bull.* 23 (1988) 51

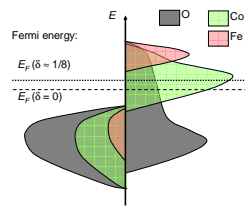
## Electronic structure

spin-projected density of states (DOS) for  
Ba<sub>0.5</sub>Sr<sub>0.5</sub>Co<sub>0.75</sub>Fe<sub>0.25</sub>O<sub>2.875</sub>



significant (Fe,Co)-O covalency (t<sub>2g</sub>)  
Fe: 1 eV gap between occupied ↑ e<sub>g</sub> and empty ↓ e<sub>g</sub>

cartoon of the BSCF band structure (density of states)

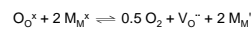
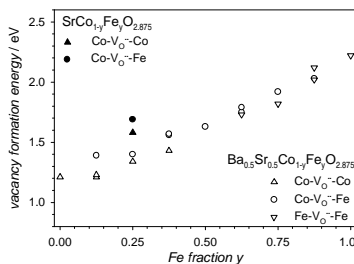


oxygen loss for δ = 1/8: excess electrons  
distributed mainly to Co and O

cf. XAS study for Ba<sub>0.1</sub>Sr<sub>0.9</sub>Co<sub>0.8</sub>Fe<sub>0.2</sub>O<sub>3-δ</sub>:  
charge distribution depends delicately on δ  
(more e to Fe at low T, high pO<sub>2</sub>)

D.N. Mueller et al.,  
*J. Mat. Chem.* 19 (2009) 1960

## Oxygen vacancy formation



BSCF = linear increase of V<sub>O</sub><sup>••</sup> formation  
energy with Fe content  
⇒ more narrow empty Fe states  
at higher energy

SCF: slightly higher values  
⇒ oversized Ba favours reduction of Fe,Co

comparison to expt. data:

E<sub>v</sub> = 0.6 eV for BSF (δ = 0.34),  
0.5 eV for BSCF (δ = 0.52)

L. Wang et al.,  
*ECS Transact.* 13(26) (2008) 85

E<sub>v</sub> depends on δ ⇒ extrapolate to δ = 1/8

trend of smaller E<sub>v</sub> for Co-rich materials confirmed

## Summary

\* vacancy formation energy increases linearly with Fe content  
⇒ difference in band structure

\* vacancy migration barriers in good agreement with experiments

\* barriers are determined by combination of

geometrical constraints (d<sub>A<sup>••</sup>-O<sup>••</sup></sub> in transition state)  
and electronic contribution (vacancy formation energy)

Vacancy formation energy E<sub>v</sub>, migration barrier E<sub>m</sub>, and structural parameters of oxygen migration.

\* indicates the migrating O and directly connected cations. Italic numbers give the change in the transition state relative to the initial state. For BSCF and SCF, the geometry and barrier from a Co-V<sub>O</sub><sup>••</sup>-Co initial state to a Co-V<sub>O</sub><sup>••</sup>-Co final state as well as for Fe-V<sub>O</sub><sup>••</sup>-Co to Fe-V<sub>O</sub><sup>••</sup>-Co (Fe<sup>••</sup>-O<sup>••</sup> transition state) is given

E <sub>v</sub>	E <sub>m</sub>	B <sup>••</sup> -O <sup>••</sup>	B <sup>••</sup> -O <sup>••</sup>	B <sup>••</sup> -O <sup>••</sup>	q(O <sup>••</sup> )	B <sup>••</sup> -O <sup>••</sup>	A <sup>••</sup> -O <sup>••</sup>	A <sup>••</sup> -O <sup>••</sup>	A <sup>••</sup> -O <sup>••</sup>
/ eV	/ eV	/ Å	/ Å	/ Å	/ e <sub>0</sub>	/ Å	/ Å	/ Å	/ Å
BSC	BaSr	1.70	1.77	1.95	-0.97	5.68	2.37	2.58	4.12
1.21	0.40	-13%	-9%	±0%	+0.10	+3%			+6%
1.03	SrSr	1.71	1.79	1.95	-0.96	5.48	2.41		4.19
	0.43	-12%	-8%	±0%	+0.11	+0%			+7%
1.28	BaBa	1.68	1.76	1.95	-0.95	5.63	2.49		4.12
	0.75	-14%	-10%	±0%	+0.12	+2%			+6%
BSCF	BaSr	1.69	1.77	1.98	-0.98	5.75	2.38	2.59	4.10
1.34	0.42	-13%	-9%	+1.5%	+0.09	+4%			+5%
1.40	C <sup>••</sup> V <sup>••</sup> -C <sup>••</sup> V <sup>••</sup>	1.69	1.76	1.91	-0.95	5.65	2.39	2.57	4.15
	0.46	-13%	-10%	-2%	+0.13	+6%			+6%
BSF	BaSr	1.68	1.78	1.95	-0.96	5.68	2.40	2.57	4.14
2.22	0.72	-14%	-9%	±0%	+0.12	+3%			+6%
SCF	SrSr	1.70	1.79	1.92	-0.97	5.56	2.38		4.08
1.58	0.60	-11%	-7%	±0%	+2%				+6%
	C <sup>••</sup> V <sup>••</sup> -C <sup>••</sup> V <sup>••</sup>	1.69	1.77	1.91	-0.97	5.52	2.38		4.11
	0.67	-11%	-8%	-2%	+2%				+7%

E. A. Kotomin, R. Merkle, Y. A. Mastrikov, M. M. Kuklja, J. Maier, *ECS Transact.* 35(1) (2011) 823; *JES* (2011) submitted

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