

Growth of High-Mobility Bi₂Te₂Se Nanoplatelets on hBN Sheets by van der Waals Epitaxy

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Supporting Information

ABSTRACT: The electrical detection of the surface states of topological insulators is strongly impeded by the interference of bulk conduction, which commonly arises due to pronounced doping associated with the formation of lattice defects. As exemplified by the topological insulator Bi_2Te_2Se , we show that via van der Waals epitaxial growth on thin hBN substrates the structural quality of such nanoplatelets can be substantially improved. The surface state carrier mobility of nanoplatelets on hBN is increased by a factor of about 3 compared to platelets on conventional Si/SiO_x substrates, which enables the observation of well-developed Shubnikov-de Haas



oscillations. We furthermore demonstrate the possibility to effectively tune the Fermi level position in the films with the aid of a back gate.

KEYWORDS: Topological insulator, magnetotransport, van der Waals epitaxy, gate tuning

S ince their theoretical prediction in 2005,¹ topological insulators (TIs) have been the subject of numerous theoretical and experimental studies. This extraordinary interest is driven by the fact that TIs are insulators in the bulk but manifest conducting helical states at their boundaries.^{1–3} In contrast to the quantum Hall state, these boundary states are the result of strong spin–orbit coupling without any external magnetic field, such that time reversal symmetry is conserved and accordingly backscattering is forbidden. The unique combination of dissipation-less charge transport channels with intrinsic spin polarization renders TIs of strong interest for spintronic applications, including spin injection^{4,5} or spin transfer torques.⁶ In addition, they hold promise for novel and exciting fundamental effects, like the formation of magnetic monopoles⁷ or Majorana fermions.⁸

While theory predicts TIs to be perfect bulk insulators, in practice their charge transport properties are dominated by defects. In fact, a sizable amount of point defects (vacancies or antisite defects) is commonly introduced during the crystal growth of the chalcogenides Bi₂Se₃, Bi₂Te₃, Sb₂Te₃ and their alloys, which represent the currently most intensively studied three-dimensional (3D) TIs. The presence of such defects leads to strong bulk doping in these compounds.^{3,9,10} Moreover, chemical reactions at the crystal surface have been documented to impart notable doping.^{11,12} The bulk doping creates a quasimetallic conduction channel parallel to the surface channels, rendering it difficult to unequivocally assign charge transport features to the topological protected surface states. Strategies that have been pursued to minimize the contribution of the bulk transport include compensation doping,^{13,14} alloying of differently doped TIs,^{15,16} or increasing the surface to bulk ratio

by using ultrathin samples.¹⁷ However, doping or alloying typically results in a concomitant drastic decrease in carrier mobility due to the introduction of defects. One possibility to avoid such decrease in the structural quality of the crystals involves the epitaxial growth of TI thin films on graphene, which has been demonstrated to significantly reduce the defect density and hence the bulk interference.¹⁸ At the same time, the lowered defect concentration in epitaxially grown films ensures enhanced carrier mobilities.¹⁹ The suitability of graphene as a substrate for epitaxial growth of TI materials derives from its layered structure with hexagonal lattice symmetry, combined with its C-C bonding length of ~1.42 Å corresponding to a small lattice mismatch of only ~2.9% versus Bi₂Se₃.^{18,25} However, due to its high electrical conductivity, graphene rules out as underlying substrate if electrical transport studies are desired on the grown TIs.

Here, we report the van der Waals epitaxial growth and electrical characterization of high quality Bi_2Te_2Se thin films on electrically insulating hexagonal boron nitride sheets (band gap of about 6 eV²⁶). Bi₂Te₂Se has emerged as one of the most promising TIs due to its simple surface band structure, large bulk band gap, and low bulk contribution to the total charge transport.^{16,20,21} Our Bi₂Te₂Se films grown by van der Waals epitaxy are sufficiently ordered to display Shubnikov-de Haas (SdH) oscillations that provide access to important quantities such as the cyclotron mass, the Fermi velocity, or Fermi energy.²³ This capability is in contrast to previously investigated

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Figure 1. van der Waals epitaxy of Bi_2Te_2Se on hBN. Schematic illustration of (a) the crystal structure of Bi_2Te_2Se and (b) the proposed epitaxial growth mode on hBN. (c) Representative AFM image of Bi_2Te_2Se nanoplatelets grown on hBN. All platelets are oriented parallel or rotated by an angle of 120° (indicated by the arrows). (d) Raman spectrum of Bi_2Te_2Se on hBN ($\lambda_{exc} = 633$ nm). The low-wavenumber region can be fitted (green curve) using three Lorentzians (blue curves). The inset amplifies the wavenumber region 1300-1450 cm⁻¹ with a Lorentzian fit to the data (green curve).



Figure 2. (a) SEM image of Bi_2Te_2Se nanoplatelets grown on hBN. The armchair and zigzag edges of the hBN sheet are marked in blue and red, respectively. (b) AFM image of the area marked in (a). (c) Histogram of the orientation distribution of the Bi_2Te_2Se nanoplatelets grown on hBN.

 Bi_2Te_2Se films grown by chemical vapor deposition (CVD) on Si/SiO_x substrates in which case the relatively low surface state mobility has prevented the observation of SdH oscillations.^{22,33} As another advantage, the present Bi_2Te_2Se films are sufficiently thin to permit tuning the Fermi level position over a wide range by applying a back gate voltage.

Bi₂Te₂Se forms rhombohedral (space group $R\overline{3}m$) crystals consisting of hexagonally close-packed atomic layers of five atoms (quintuple layer) arranged along the *c*-axis as follows: Se⁽¹⁾/Te⁽¹⁾-Bi-Se⁽²⁾/Te⁽²⁾-Bi-Se⁽¹⁾/Te⁽¹⁾ (see Figure 1a), with the lattice constants a = 4.283 Å and c = 29.846 Å.²⁴ Hexagonal boron nitride (hBN), which likewise forms a layered crystal with hexagonal symmetry, has a lattice constant of 1.45 Å, close to that of graphene. The alignment of Bi₂Te₂Se on hBN proposed in Figure 1b is characterized by a small lattice mismatch of 1.5%. In addition, the layered crystal structure of Bi₂Te₂Se and hBN promotes epitaxial growth by van der Waals epitaxy. Herein, the weak van der Waals interaction between the two materials relaxes the lattice-mismatch condition.²⁵

Thin Bi₂Te₂Se films were grown by a catalyst free vapor solid method,^{27,33} using a horizontal tube furnace equipped with a quartz tube (tube diameter 2.5 cm). First, ultrapure Bi₂Se₃ and Bi₂Te₃ crystalline powders (Alfa Aesar, 99.999%) were placed in the hot zone of the furnace. The hBN growth substrates were then prepared by micromechanical cleavage of hBN powder on Si/SiO_x substrates and mounted ~15 cm away from the hot zone within the colder downstream region. The tube was evacuated repeatedly down to a pressure of p < 1 mbar and flushed with ultrapure Argon to remove oxygen, followed by adjusting the Argon flow to 150 sccm and the pressure in the tube to 80 mbar. Subsequently, the furnace was heated to approximately 590 °C and held at this temperature for 30 s to 6 min, followed by natural cool down without gas flow. Morphology and thickness of the films were found to sensitively depend on the position of the growth substrates and the growth time. The accessible thickness was determined to range between 4 and 500 nm.

As exemplified by the AFM images in Figure 1c and Figure 2b, as well as the SEM image in Figure 2a, Bi₂Te₂Se grows on top of the hBN in the form of regular platelets with hexagonal symmetry. The Bi2Te2Se growth mechanism proposed in Figure 1b is supported by the observation that the crystal faces in all platelets are oriented parallel or rotated by 60 or 120° (see Figure 2c). In addition, it can be seen in Figure 2a that the nanoplatelets preferably grow parallel to one of the sharp edges of the hBN sheet that are formed during exfoliation. Because the edges of the hBN flake enclose an angle of precisely 30°, they can be assigned to armchair or zigzag edges. Assuming that the edges marked in blue in Figure 2a are the armchair edges of the hBN flakes, the growth mechanism suggested in Figure 1b gains further support (if these edges were the zigzag edges instead, the resulting misfit would be unrealistically high, specifically 26% in case that the Bi₂Te₂Se flakes would be compressed, and 47% if they would be expanded).

Evidence for the formation of Bi_2Te_2Se could be gained by Raman spectroscopy. The chalcogenides Bi_2Se_3 , Bi_2Te_3 , and their alloys $Bi_2(Se_xTe_{1-x})_3$ are highly Raman active in the low wavenumber region.²⁸ The Raman spectrum in Figure 1d, acquired with a laser wavelength of 633 nm, displays three peaks at 105.0, 139.1, and 149.6 cm⁻¹, respectively. They can be identified as the E_g^2 and the A_{1g}^2 peak (which is split into two components) of $Bi_2Te_2Se.^{28}$ The additional peak at 1365.5 cm⁻¹ (see Figure 1d, inset) corresponds to the E_{2g} mode of the underlying hBN flake.²⁹ It is noteworthy that besides $Bi_2Te_2Se_3$ also Bi_2Se_3 could be grown on hBN by van der Waals epitaxy (see Supporting Information).

For electrical transport studies, standard e-beam lithography was performed to provide individual Bi_2Te_2Se platelets with Ti(4 nm)/Au(200 nm) contacts in Hall bar or van der Pauw geometry. Figure 3a displays the high field part of the Hall



Figure 3. (a) High-field Hall resistance (black curve) and its first derivative (green curve) as a function of the magnetic field showing pronounced SdH oscillations. (b) Amplitude of the SdH oscillations as a function of $1/[B \cos(\theta)]$ for different tilting angles θ (between surface normal and magnetic field). The inset shows the position *B* of the SdH peak with the LL index n = 22 (arrow) for different angles θ , combined with a $1/\cos \theta$ fit (green curve) to the data.

resistance R_{xy} as a function of the magnetic field *B* at T = 1.5 K for a 45 nm thick Bi₂Te₂Se platelet on a ~50 nm thick hBN sheet. The R_{xy} signal clearly features SdH oscillations, as highlighted by the first derivative dR_{xy}/dB in Figure 3a. In a prototypic two-dimensional (2D) electron gas, SdH oscillations are periodic in 1/B, with a periodicity given by²³

$$2\pi n = A_{\rm F} \frac{\hbar}{eB} \tag{1}$$

where *n* is the Landau level (LL) index, and $A_{\rm F}$ is the external cross-section of the Fermi surface. For 2D electron systems, the formation of LLs depends only on the B-field component $B_{\perp} = B \cos(\theta)$ normal to the surface. Accordingly, if the observed quantum oscillations originated from the topological 2D surface states, the maxima/minima of the SdH oscillations should shift by $1/[B\cos(\theta)]$ upon tilting the sample in the magnetic field B. Indeed, in the plot of the amplitude of the SdH oscillations $\Delta R_{xy} (= R_{xy} - \langle R_{xy} \rangle$, where $\langle R_{xy} \rangle$ is a smoothed background) as

a function of B_{\perp} in Figure 3b, all curves coincide up to an angle of 50°. To further underscore the 2D character, the inset of Figure 3b demonstrates that the dependence of the position of the n = 22 peak at B = 7.7 T (for $\theta = 0^{\circ}$) on the tilting angle θ can be smoothly fitted with a $1/\cos(\theta)$ function.

Having confirmed the 2D nature of the SdH oscillations, we now address the position of the Fermi level in our samples. The Fermi energy can be calculated from

$$E_{\rm F} = m_{\rm cyc} v_{\rm F}^2 \tag{2}$$

where m_{cyc} is the cyclotron mass and v_F is the Fermi velocity. According to the Lifshitz–Kosevich (LK) theory³⁰ the thermal damping of the SdH oscillations provides a suitable estimate for the cyclotron mass m_{cyc} . From the plot of ΔR_{xy} versus 1/*B* at different temperatures in Figure 4a, the oscillation amplitude is



Figure 4. (a) Amplitude of the SdH oscillations as a function of 1/B for different temperatures and (b) the normalized amplitude of the SdH maximum with the LL index n = 15 (arrow) as a function of temperature. The data fit (solid line) was obtained using the Lifshitz–Kosevich theory (see main text).

seen to decrease with increasing temperature. Figure 4b displays the amplitude of the n = 15 peak at B = 11 T, normalized according to the LK formula

$$\frac{\Delta\sigma_{xy}(T)}{\Delta\sigma_{xy}(0)} = \frac{\lambda(T)}{\sinh\lambda(T)}$$
(3)

where $\lambda(T) = 2\pi^2 k_{\rm B} T m_{\rm cyc}/(\hbar eB)$. Fitting of the data yields a value of $m_{\rm cyc}/m_0 = 0.15$, which agrees well with previous reports on Bi₂Te₂Se bulk crystals.²⁰ Furthermore, in order to access the Fermi vector $k_{\rm F}$ we plot the position 1/B of the SdH maxima as

a function of the LL index *n* (see Figure 5b below). The LL index is obtained by plotting the SdH maxima as a function of n + 1/4 (since we are using the R_{xy} signal, see Supporting Information) and extrapolating to $1/B \rightarrow 0$ (i.e., $B \rightarrow \infty$). The intersection with the abscissa defines the first LL. By fitting the data with the Onsager relation (eq 1) and assuming a circular 2D Fermi surface with $A_{\rm F} = \pi k_{\rm F}^2$ one obtains a value of $k_{\rm F} = 0.073$ Å⁻¹. On this basis, a surface carrier density of 4.2×10^{16} m⁻² is calculated from $n_{\rm s} = k_{\rm F}^2/4\pi$. This value agrees well with the surface carrier density of 5.4×10^{16} m⁻², as derived from Hall measurements (see Supporting Information), thus further supporting the 2D nature of the SdH oscillations.

Toward determining the Fermi energy using eq 2, we assume Dirac fermions with linear dispersion relation and a Fermi velocity of $v_{\rm F} = \hbar k_{\rm F}/m_{\rm cyc} = 5.7 \times 10^5$ m/s, which is close to the value of $v_{\rm F} = 4.6 \times 10^5$ m/s determined by ARPES.¹⁶ On this basis, a Fermi energy of $E_{\rm F}$ = 272 meV above the Dirac point is obtained. By comparison, a value of $E_{\rm F}$ = 223 meV is derived for $k_{\rm F} = 0.073$ Å⁻¹ from the ARPES-derived band structure.¹⁶ We have furthermore tested the possibility to tune the Fermi level in our samples through the action of a back gate. As can be discerned from Figure 5a, which displays the extracted SdH oscillations for different back gate voltages $V_{\rm C}$, the period $\Delta 1/B$ rises with increasing $V_{\rm G}$. In Figure 5b, the peak positions of the SdH oscillations are plotted as a function of the LL index n. As discussed above, the slopes directly yield values for the Fermi vector $k_{\rm F}$ via eq 1. The corresponding $E_{\rm F}$ values can then be determined with the aid of the ARPES-derived band structure of Bi_2Te_2Se , see Figure 5c.¹⁶ In this manner, the error associated with the assumptions made to calculate the cyclotron mass can be avoided (for comparison, Supporting Information Figure S5 shows $E_{\rm F}$ values derived from the cyclotron mass). The sketch in Figure 5d evidences that $E_{\rm F}$ (of the bottom surface which is influenced by the back gate, see arguments below) can be shifted by approximately 160 meV through the back gate voltage. Similar Fermi level shifts have been observed in case of considerably thicker hBN sheets ($\approx 200 \text{ nm}$), which is in accordance with the estimated gate capacitances (see Supporting Information). The application of a gate voltage is expected to cause bending of the bands at the interface between dielectric (hBN) and semiconductor (Bi₂Te₂Se), and thus to create a depletion layer. The thickness of the latter, which corresponds to the penetration depth of the electric field in the semiconductor, is of the order of only 10 nm.³¹ Accordingly, the bulk and the top surface of the platelet should be only little affected by gating.

The fact that the SdH oscillations show only a single period for all gate voltages (see Figure 4b), indicates the contribution of only one surface state. A similar conclusion has recently been drawn from the magnetotransport behavior of Bi₂Te₂Se nanoplatelets on Si/SiO_x.³³ We attribute this finding to a deterioration of the surface state at the top surface due to long exposure to air, an explanation which is in accordance with previous charge transport studies on Bi₂Se₃.^{12,14} Moreover, the results of low-temperature Hall measurements performed at different back gate voltages (see Supporting Information) are consistent with the *n*-doped character of our samples.^{20–22} It is furthermore noteworthy that the Hall mobilities agree well with the values extracted from the SdH oscillations for $-60 \text{ V} < V_g < 20 \text{ V}$ (see Supporting Information).

We attribute the very high surface state carrier mobility in the range of 8 000 to 20 000 $\text{cm}^2/(\text{V s})$ to the reduced defect density in the films grown by van der Waals epitaxy. This



Figure 5. (a) Amplitude of the SdH oscillations as a function of 1/B for different back gate voltages. (b) Plot of LL index 1/B versus number of maximum for different gate voltages. The data fits (solid lines) were performed using eq 1. (c) Calculated Fermi energy as a function of back gate voltage. (d) Sketch of the position of the Fermi level of the bottom surface in the Bi₂Te₂Se samples for different back gate voltages.

assertion gains support by comparing Bi_2Te_2Se thin films grown on hBN or Si/SiO_x substrates (see Supporting Information). Specifically, an average surface state mobility of ~4900 cm²/(V s) was determined for Bi_2Te_2Se on hBN, approximately three times larger than the value of 1600 cm²/(V s) obtained in case of the Si/SiO_x substrates.

In summary, we have successfully grown the topological insulator Bi_2Te_2Se on hBN in an oriented manner by van der Waals epitaxy. Thus obtained thin films show enhanced surface mobilities, which enable the study of gate-dependent quantum oscillations for the first time in this material. The unique combination of high mobility surface charge transport with an efficient tunability of the Fermi level provides a suitable basis for studying novel, spin-related charge transport phenomena in such devices.

ASSOCIATED CONTENT

S Supporting Information

Details on preparation of hBN flakes; additional AFM and Raman data for Bi_2Te_2Se films on hBN; growth of Bi_2Se_3 on hBN; Hall data for the device discussed in the main text and another device; calculation of the surface mobility from SdH data; estimation of gate capacitance; comparison of Fermi energy, as derived from ARPES band structure and SdH oscillations; model for surface state mobility as a function of carrier density; comparison between R_{xx} and R_{xy} ; Hall data for a 12 nm thin sample. This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes

The authors declare no competing financial interest.

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