High-temperature superconductivity, which occurs by carrier doping to a copper oxide (cuprate) Mott insulator, is one of the most significant discoveries in 20th-century physics. Immediately after its discovery, attention was given to the anomalous behaviours of various physical properties observed above the superconducting transition temperature \( T_c \). The electronic state relevant to these is a pseudogap, which opens above \( T_c \) in the density of states close to the Fermi level. The pseudogap was first discovered in the measurement of nuclear magnetic relaxation (NMR) rate \( 1/T_1 \) at high temperatures following the Curie-Weiss law, whereas, on cooling, it becomes peaked at a certain temperature much higher than \( T_c \) and then begins to decrease. This phenomenon was called “spin gap” because a gap seems to appear in the spin excitation spectrum. An energy gap was later found to open at temperatures higher than \( T_c \) in the density of states near the Fermi level by photoelectron spectroscopy and tunnelling spectroscopy, and since then, this gap has been called “pseudogap”.

In the underdoped regime close to the Mott insulating phase, theory predicted the formation of “small Fermi pocket”. However, an arc-shaped Fermi surface, that can be defined neither as a “large Fermi surface” nor as a “small Fermi pocket”, was observed, due to the opening of the pseudogap at partial segments of the Fermi surface. The Fermi-arc is a strange electronic state, and understanding the relation of the pseudogap with the superconductivity has been thought of as crucial to elucidate the mechanism of high-\( T_c \) superconductivity. On this issue, two controversial views have been given: the first is that the pseudogap arises due to the pair formation of electrons as a precursor phenomenon of superconductivity. The second is that the pseudogap is, in contrast, generated by an electronic state distinct from preformed pairs, such as charge order or charge density wave, which compete with superconductivity.

In my talk, I will introduce my study of the pseudogap state in cuprates by high-resolution angle-resolved photoelectron spectroscopy (ARPES), clearly demonstrating that the pseudogap state competes with superconductivity. I will also present the successful observation of a “small Fermi pocket” near the Mott phase. The investigation of the lightly-doped Mott state may lead to the elucidation of the relationship between the Fermi arc and small Fermi pocket in cuprates, which has been a theoretical difficulty for many years. Importantly, the substitution of elements for carrier doping causes significant inhomogeneity in electronic states, making it hard to investigate the intrinsic electronic properties of the lightly-doped Mott state. The multi-layered cuprates focused on in my study has inner CuO₂ planes avoiding direct contact with charge reservoir layers, which realize a clean electronic system without the disorder. These compounds became the key to our successful observation of “small Fermi pockets”, which could allow further development of the study of cuprates, as will be discussed in my lecture.